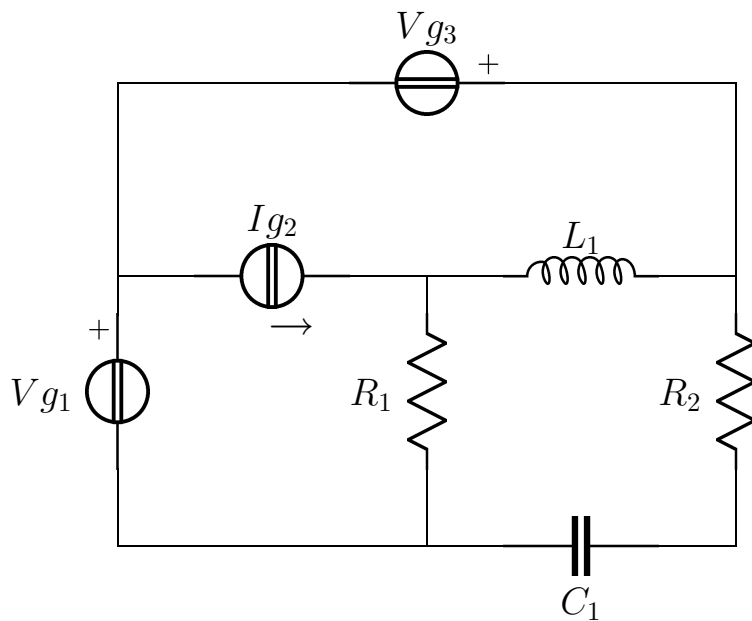


Esercizio A1

Risolvere il circuito in figura



$$\begin{aligned} \mathbf{V}_{g1} &= \frac{3}{2} - 2j \\ R_1 &= 2 \\ R_2 &= \frac{1}{2} \\ C_1 &= \frac{1}{5} \\ \mathbf{I}_{g2} &= 1 \\ L_1 &= \frac{1}{2} \\ \mathbf{V}_{g3} &= \frac{3}{2} \\ \omega &= 2 \end{aligned}$$

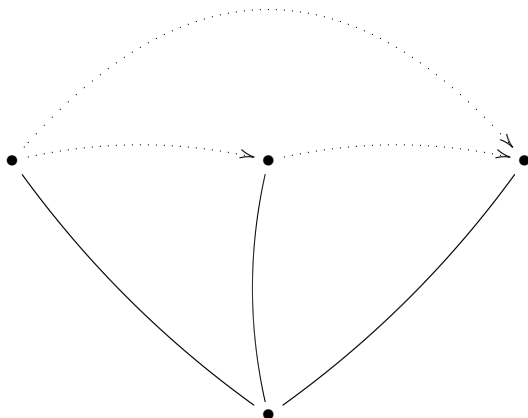
Semplificazioni serie/parallelo

$$Z_a = R_2 + \frac{1}{j\omega C_1} = \frac{1}{2} - \frac{5}{2}j$$

$$Y_a = \frac{1}{13} + \frac{5}{13}j$$

Risoluzione dell'esercizio con il metodo delle maglie

Albero e coalbero:



Sistema

$$\left\{ \begin{array}{rcl} R_1 \mathbf{I}_1 & -R_1 \mathbf{I}_2 & = \mathbf{V}_{g1} + \mathbf{V}_{x2} \\ -R_1 \mathbf{I}_1 & +(R_1 + Z_a + j\omega L_1) \mathbf{I}_2 & + Z_a \mathbf{I}_3 = 0 \\ & Z_a \mathbf{I}_2 & + Z_a \mathbf{I}_3 = \mathbf{V}_{g1} + \mathbf{V}_{g3} \\ \mathbf{I}_1 & & = \mathbf{I}_{g2} \end{array} \right.$$

Sostituzione

$$\left\{ \begin{array}{rcl} 2\mathbf{I}_1 & -2\mathbf{I}_2 & = \frac{3}{2} - 2j + \mathbf{V}_{x2} \\ -2\mathbf{I}_1 & +(\frac{5}{2} - \frac{3}{2}j)\mathbf{I}_2 & +(\frac{1}{2} - \frac{5}{2}j)\mathbf{I}_3 = 0 \\ & (\frac{1}{2} - \frac{5}{2}j)\mathbf{I}_2 & +(\frac{1}{2} - \frac{5}{2}j)\mathbf{I}_3 = 3 - 2j \\ \mathbf{I}_1 & & = 1 \end{array} \right.$$

Soluzione

$$\left\{ \begin{array}{rcl} \mathbf{I}_1 & = & 1 \\ \mathbf{I}_2 & = & j \\ \mathbf{I}_3 & = & 1 \\ \mathbf{V}_{x2} & = & \frac{1}{2} \end{array} \right.$$

Bilancio di potenza

Potenza complessa erogata dai generatori:

$$\begin{aligned} \mathbf{I}_{V_{g1}} &= \mathbf{I}_1 + \mathbf{I}_3 = 2 & P_{c_{V_{g1}}} &= \frac{1}{2} \mathbf{V}_{g1} \mathbf{I}_{V_{g1}}^* = \frac{3}{2} - 2j \\ \mathbf{V}_{I_{g2}} &= \mathbf{V}_{x2} = \frac{1}{2} & P_{c_{I_{g2}}} &= \frac{1}{2} \mathbf{V}_{I_{g2}} \mathbf{I}_{g2}^* = \frac{1}{4} \\ \mathbf{I}_{V_{g3}} &= \mathbf{I}_3 = 1 & P_{c_{V_{g3}}} &= \frac{1}{2} \mathbf{V}_{g3} \mathbf{I}_{V_{g3}}^* = \frac{3}{4} \end{aligned}$$

$$P_{c_{tot}} = \frac{5}{2} - 2j$$

Potenza attiva assorbita dai resistori:

$$\begin{aligned} \mathbf{I}_{R1} &= -\mathbf{I}_1 + \mathbf{I}_2 = -1 + j & P_{a_{R1}} &= \frac{1}{2} R_1 |\mathbf{I}_{R1}|^2 = 2 \\ \mathbf{I}_{R2} &= -\mathbf{I}_2 - \mathbf{I}_3 = -1 - j & P_{a_{R2}} &= \frac{1}{2} R_2 |\mathbf{I}_{R2}|^2 = \frac{1}{2} \end{aligned}$$

$$P_{a_{tot}} = \frac{5}{2} = \Re\{P_{c_{tot}}\}$$

Potenza reattiva assorbita dai condensatori e induttori:

$$\begin{aligned} \mathbf{I}_{L_1} &= \mathbf{I}_2 = j & Q_{L_1} &= \frac{1}{2}\omega L_1 |\mathbf{I}_{L_1}|^2 = \frac{1}{2} \\ \mathbf{V}_{C_1} &= \frac{-\mathbf{I}_2 - \mathbf{I}_3}{j\omega C_1} = -\frac{5}{2} + \frac{5}{2}j & Q_{C_1} &= -\frac{1}{2}\omega C_1 |\mathbf{V}_{C_1}|^2 = -\frac{5}{2} \\ Q_{tot} &= -2 = \Im m\{P_{c_{tot}}\} \end{aligned}$$

Soluzioni:

$$\begin{aligned} V_{g_1} &= \frac{3}{2} - 2j; & I_{g_1} &= 2; & Pc_{V_{g_1}} &= \frac{3}{2} - 2j \\ V_{R_1} &= 2 - 2j; & I_{R_1} &= -1 + j; & Pa_{R_1} &= 2 \\ V_{R_2} + V_{C_1} &= 3 - 2j; & I_{R_2} = I_{C_1} &= -1 - j; & Pa_{R_2} &= \frac{1}{2} \\ Q_{C_1} &= -\frac{5}{2} \\ V_{g_2} &= \frac{1}{2}; & I_{g_2} &= 1; & Pc_{I_{g_2}} &= \frac{1}{4} \\ V_{L_1} &= 1; & I_{L_1} &= j; & Q_{L_1} &= \frac{1}{2} \\ V_{g_3} &= \frac{3}{2}; & I_{g_3} &= 1; & Pc_{V_{g_3}} &= \frac{3}{4} \end{aligned}$$