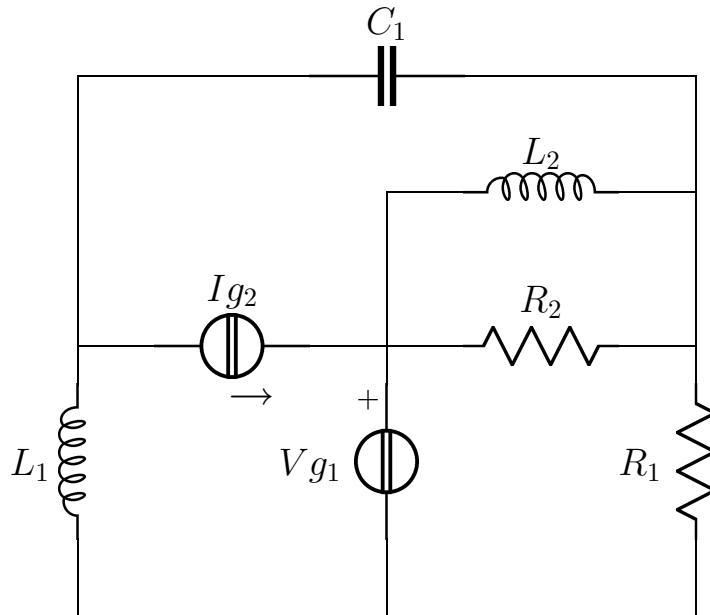


Esercizio ggcesame2015 – 02 – 24B4Maglie

Risolvere il circuito in figura



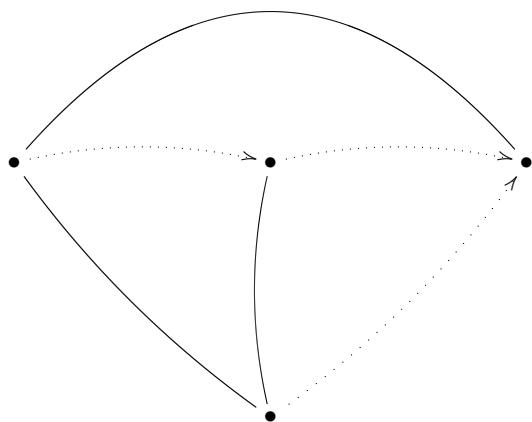
$$\begin{aligned}
 L_1 &= 1 \\
 \mathbf{V}_{g_1} &= -j \\
 R_1 &= 1 \\
 \mathbf{I}_{g_2} &= -1 - 3j \\
 R_2 &= 2 \\
 L_2 &= \frac{2}{7} \\
 C_1 &= 2 \\
 \omega &= 1
 \end{aligned}$$

Semplificazioni serie/parallelo

$$\begin{aligned}
 Y_a &= \frac{1}{R_2} + \frac{1}{j\omega L_2} = \frac{1}{2} - \frac{7}{2}j \\
 Z_a &= \frac{1}{25} + \frac{7}{25}j
 \end{aligned}$$

Risoluzione dell'esercizio con il metodo delle maglie

Albero e coalbero:



Sistema

$$\left\{ \begin{array}{lcl} (j\omega L_1 + R_1 + \frac{1}{j\omega C_1})\mathbf{I}_1 & -j\omega L_1 \mathbf{I}_2 & +(j\omega L_1 + \frac{1}{j\omega C_1})\mathbf{I}_3 = 0 \\ -j\omega L_1 \mathbf{I}_1 & +j\omega L_1 \mathbf{I}_2 & -j\omega L_1 \mathbf{I}_3 = -\mathbf{V}_{g_1} + \mathbf{V}_{x_2} \\ (j\omega L_1 + \frac{1}{j\omega C_1})\mathbf{I}_1 & -j\omega L_1 \mathbf{I}_2 & +(j\omega L_1 + Z_a + \frac{1}{j\omega C_1})\mathbf{I}_3 = \mathbf{V}_{g_1} \\ & \mathbf{I}_2 & = \mathbf{I}_{g_2} \end{array} \right.$$

Sostituzione

$$\left\{ \begin{array}{lcl} (1 + \frac{1}{2}j)\mathbf{I}_1 & -j\mathbf{I}_2 & +\frac{1}{2}j\mathbf{I}_3 = 0 \\ -j\mathbf{I}_1 & +j\mathbf{I}_2 & -j\mathbf{I}_3 = j + \mathbf{V}_{x_2} \\ \frac{1}{2}j\mathbf{I}_1 & -j\mathbf{I}_2 & +(\frac{1}{25} + \frac{39}{50}j)\mathbf{I}_3 = -j \\ & \mathbf{I}_2 & = -1 - 3j \end{array} \right.$$

Soluzione

$$\left\{ \begin{array}{lcl} \mathbf{I}_1 & = & 1 \\ \mathbf{I}_2 & = & -1 - 3j \\ \mathbf{I}_3 & = & -3 - 4j \\ \mathbf{V}_{x_2} & = & -1 \end{array} \right.$$

Bilancio di potenza

Potenza complessa erogata dai generatori:

$$\begin{aligned} \mathbf{I}\mathbf{V}_{g_1} &= -\mathbf{I}_2 + \mathbf{I}_3 = -2 - j & P_{c_{V_{g_1}}} &= \frac{1}{2}\mathbf{V}_{g_1}\mathbf{I}_{V_{g_1}}^* = \frac{1}{2} + j \\ \mathbf{V}_{I_{g_2}} &= \mathbf{V}_{x_1} = -1 & P_{c_{I_{g_2}}} &= \frac{1}{2}\mathbf{V}_{I_{g_2}}\mathbf{I}_{g_2}^* = \frac{1}{2} - \frac{3}{2}j \end{aligned}$$

$$P_{c_{tot}} = 1 - \frac{1}{2}j$$

Potenza attiva assorbita dai resistori:

$$\begin{aligned} \mathbf{I}_{R_1} &= \mathbf{I}_1 = 1 & P_{a_{R_1}} &= \frac{1}{2}R_1|\mathbf{I}_{R_1}|^2 = \frac{1}{2} \\ \mathbf{I}_{R_2} &= \frac{\mathbf{I}_3 Z_a}{R_2} = \frac{1}{2} - \frac{1}{2}j & P_{a_{R_2}} &= \frac{1}{2}R_2|\mathbf{I}_{R_2}|^2 = \frac{1}{2} \end{aligned}$$

$$P_{a_{tot}} = 1 = \Re\{P_{c_{tot}}\}$$

Potenza reattiva assorbita dai condensatori e induttori:

$$\begin{aligned}
 \mathbf{I}_{\mathbf{L}_1} &= -\mathbf{I}_1 + \mathbf{I}_2 - \mathbf{I}_3 = 1 + j & Q_{L_1} &= \frac{1}{2}\omega L_1 |\mathbf{I}_{\mathbf{L}_1}|^2 = 1 \\
 \mathbf{V}_{\mathbf{C}_1} &= (-\mathbf{I}_1 - \mathbf{I}_3) \frac{1}{j\omega C_1} = 2 - j & Q_{C_1} &= -\frac{1}{2}\omega C_1 |\mathbf{V}_{\mathbf{C}_1}|^2 = -5 \\
 \mathbf{I}_{\mathbf{L}_2} &= \frac{\mathbf{I}_3 Z_a}{j\omega L_2} = -\frac{7}{2} - \frac{7}{2}j & Q_{L_2} &= \frac{1}{2}\omega L_2 |\mathbf{I}_{\mathbf{L}_2}|^2 = \frac{7}{2} \\
 Q_{tot} &= -\frac{1}{2} = \Im m\{P_{c_{tot}}\}
 \end{aligned}$$

Soluzioni:

$$\begin{aligned}
 V_{L_1} &= 1 - j; & I_{L_1} &= 1 + j; & Q_{L_1} &= 1 \\
 V_{g_1} &= -j; & I_{g_1} &= -2 - j; & P_{cV_{g_1}} &= \frac{1}{2} + j \\
 V_{R_1} &= -1; & I_{R_1} &= 1; & P_{aR_1} &= \frac{1}{2} \\
 V_{g_2} &= -1; & I_{g_2} &= -1 - 3j; & P_{cI_{g_2}} &= \frac{1}{2} - \frac{3}{2}j \\
 V_{R_2} &= V_{L_2} = -1 + j; & I_{R_2} + I_{L_2} &= -3 - 4j; & P_{aR_2} &= \frac{1}{2} \\
 Q_{L_2} &= \frac{7}{2} \\
 V_{C_1} &= -2 + j; & I_{C_1} &= 2 + 4j; & Q_{C_1} &= -5
 \end{aligned}$$